

Full name(s): \_\_\_\_\_ .

*Questions*

1. Compute derivative of  $\tan(x)$  by writing it in terms of  $\sin(x)$  and  $\cos(x)$  and using the quotient rule. Simplify.
2. Do the same for  $\sec(x)$ ,  $\csc(x)$ , and  $\cot(x)$ .
3. Use the derivative rule for inverse functions to compute:
  - $\frac{d}{dx} \cos^{-1}(x)$ .
  - $\frac{d}{dx} \tan^{-1}(x)$ .
  - $\frac{d}{dx} \sec^{-1}(x)$ .
  - $\frac{d}{dx} \csc^{-1}(x)$ .
  - $\frac{d}{dx} \cot^{-1}(x)$ .
4. Compute derivatives of:
  - $\sin(\ln(x))$
  - $\ln(1 + \sin(x))$
  - $\tan^{-1}(\sqrt{x^2 + 1})$
  - $\ln \frac{2^x - 1}{2^x + 1}$
  - $\sin^{-1}\left(\frac{2}{\pi} \frac{x^2}{x^2 + 1}\right)$
5. Compute the second derivatives of:
  - $f(x) = \frac{1}{x}$ .
  - $f(x) = \sin(x)$
  - $f(x) = e^4 x$
  - $f(x) = \frac{x+1}{x-1}$
6. A ball is moving with trajectory  $x(t) = 10t$  and  $y(t) = 8t - 5t^2$ . What is the ball's vertical acceleration?
7. A spherical balloon is being inflated so that its surface area is increasing at  $1 \text{ cm}^2/\text{s}$ . How fast is its volume increasing?